

Register Number:

Name of the Candidate:

B.Sc. DEGREE EXAMINATION, May 2015**(COMPUTER SCIENCE)****(FIRST YEAR)****(PART-III)****130/140: SCIENTIFIC COMPUTING**

(Common with B.Sc I.T and B.C.A)

Time: Three hours

Maximum: 100 marks

Answer any FIVE questions (5×20=100)

1. a) Solve for a positive root of $x - \cos x = 0$ by regular falsi method. (10)
 b) Using Gauss-Seidal method, solve the following system. Start with $x=1, y=2, z=3$ (10)

$$x + 3y + 5z = 173.61$$

$$x - 27y + 2z = 71.31$$

$$41x - 2y + 3z = 65.46$$

2. a) Apply Gauss-Jordan method, to solve the system. (10)
- $$8x - 3y + 2z = 20$$
- $$4x + 11y - z = 33$$
- $$6x + 3y + 12z = 35$$
- b) Find the least positive root of the equation $\tan x = x$ to an accuracy of 0.0001 by Newton-Raphson method. (10)

3. a) Compute $f'(0)$ and $f''(4)$ from the data. (10)

x	0	1	2	3	4
y	1	2.718	7.381	20.086	54.598

- b) Find the value of y at $x=21$ from the following data. (10)

x	20	23	26	29
y	0.3420	0.3907	0.4384	0.4848

4. a) Find the First, Second and Third derivatives of $f(x)$ at $x=1.5$ if, (10)

x	1.5	2.0	2.5	3.0	3.5	4.0
F(x)	3.375	7.000	13.625	24.000	38.875	59.000

- b) Evaluate (10)

$$\int_0^5 \frac{dx}{4x+5}$$

by Simpson's one-third rule and hence find the value of $\log_e 5(n=10)$

5. a) Using Taylor's series method find y at $x=1.1$ and 1.2 by solving, (10)

$$\frac{dy}{dx} = x^2 + y^2 \text{ given } y(1)=2.3$$

- b) Find an approximate solution of the initial value problem, (10)

$$y' = 1 + y^2, y(0) = 0$$

by Picard's method

6. a) Using Euler's method. (10)

$$\text{Solve } \frac{dy}{dx} = 1 + xy \text{ with } y(0) = 2$$

Find $y(0.1)$, $y(0.2)$ and $y(0.3)$

- b) Compute $y(0.1)$ and $y(0.2)$ by Runge-Kutta 4th order for the (10)
differential equation.

$$\frac{dy}{dx} = xy + y^2, y(0) = 1$$

7. a) Classify the equations. (10)

i) $U_{xx} + 2u_{xy} + u_{yy} = 0$

ii) $x^2 f_{xx} + (1-y^2) f_{yy} = 0$

- b) Solve, (10)

$$\frac{\partial^2 u}{\partial x^2} - 2 \frac{\partial u}{\partial t} = 0$$

Given $u(0,t) = 0$, $u(4,t) = 0$

$$U(x,0) = x(4-x)$$

Assume $h=1$

Find the values of u up to $t=5$

8. a) Solve the Laplace equation at the interior points of the square region (10)
given below:

	500	1000	1000	1000	500
0		47	48	49	0
0		44	45	46	0
0		41	42	43	0
	0	0	0		

- b) Compare Trapezoidal rule and Simpson's 1/3 rule for evaluating numerical integration. (5)
